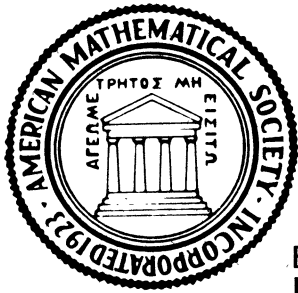


# Mathematics of Computation



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July 1979

Volume 33, Number 147, Pages 849–1124

**Published by the American Mathematical Society  
Providence, Rhode Island USA**

ISSN 0025-5718

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